

# A Pricing App Using Regularized GLMs to Enhance Risk Modeling in P&C

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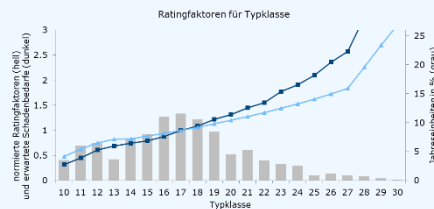
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# In a Nutshell

## A Classical Pricing Process in Motor

**Typical:  
GLM**

**Net Risk Premium**  
= Base Level × Rating Factors



**Risk Modeling**  
via iterative fitting of multivariate  
models to derive best estimates of  
individual claims expectancies in  
the modeling portfolio

### Tariff Modeling

Tariff portfolio, costs and margins, market positioning  
Legal and regulatory frameworks  
Rating factors: Spread, damping, offsets, structure, ...



**Data Preprocessing:**  
analyses, validation,  
cleansing, adjustments, ...



**Building Blocks:**  
lines of business,  
claim types,  
claim components, ...

Data Sources

Feature  
Preselection

Separate Models:  
inflation, trends,  
large losses, ...

Adjustments:  
base level, portfolio,  
product design, costs,  
safety and profit  
margins, discounts  
and rebates, ...

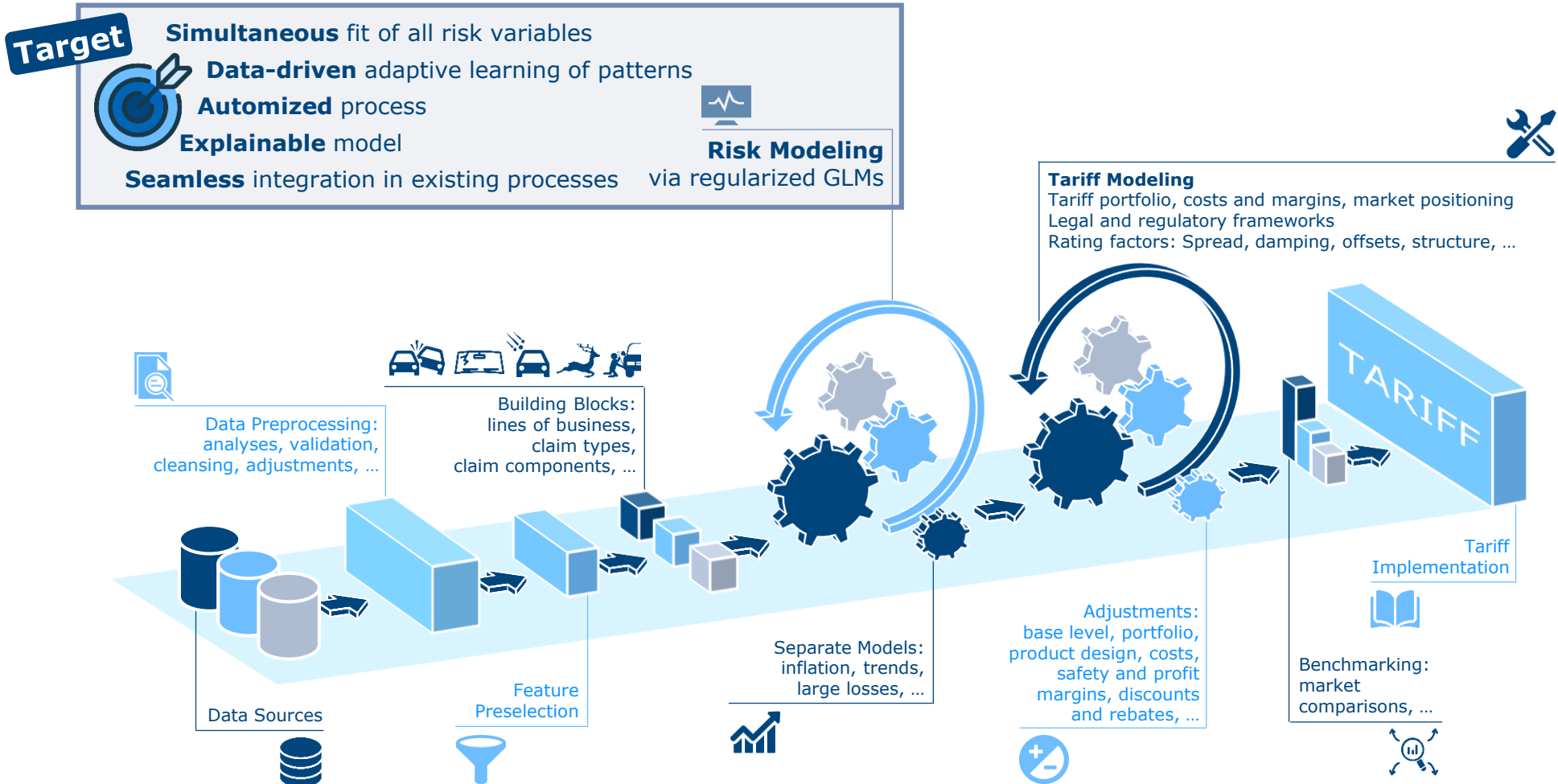
Tariff  
Implementation

Benchmarking:  
market  
comparisons, ...



# In a Nutshell

## A Classical Pricing Process in Motor



# GLM Regularization

## Punish the Complexity!

### Definition: Generalized Linear Model (GLM)



|                          |                                                                                          |
|--------------------------|------------------------------------------------------------------------------------------|
| Probability distribution | $f(Y; \theta, \phi) = \exp \left( \frac{Y\theta - b(\theta)}{\phi} + c(Y; \phi) \right)$ |
| Link function            | $g: \mathbb{R} \rightarrow \mathbb{R}$ s.th. $\eta = g(\mu)$ with $\mu = \mathbb{E}(Y)$  |
| Linear predictor         | $\eta = X\beta = \beta_0 + \beta_1 X_1 + \dots + \beta_m X_m$                            |

#### Standard

Estimate  $\beta$  using maximum likelihood:

$$\ell(\beta; y_i, x_i) = -\frac{1}{n} \sum_{i=1}^n \log f(y_i | x_i, \beta) \rightarrow \min$$

#### Extra

Introduce penalty term to punish complexity (reduce overfitting):

$$\ell_{\text{pen}}(\beta; y_i, x_i, \lambda) = \ell(\beta; y_i, x_i) + \lambda \Omega(\beta_1, \dots, \beta_m) \rightarrow \min$$

Components:

**Regularization Parameter**  $\lambda \geq 0$  to balance

- punishment  $\Omega(\beta_1, \dots, \beta_m)$  of complexity and
- fit of likelihood  $\ell(\beta; y_i, x_i)$  to the data

**Penalty Function**  $\Omega: \mathbb{R}^m \rightarrow \mathbb{R}_+$   
for parameters  $\beta_1, \dots, \beta_m$   
(without intercept)

Technical prerequisites: Standardize variables  $x_i$  to allow for comparison of the magnitude of  $\beta$

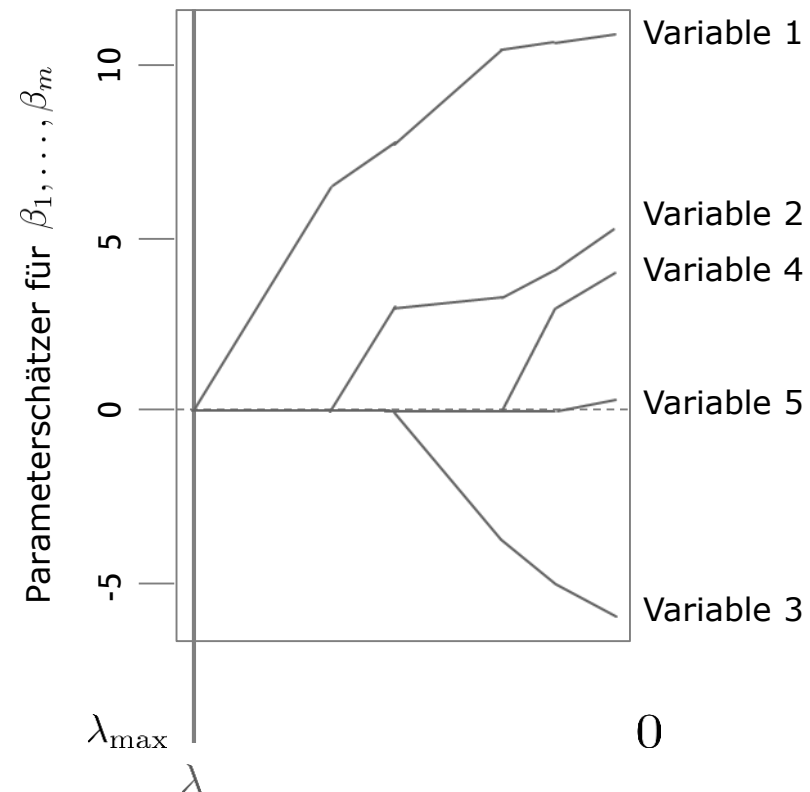
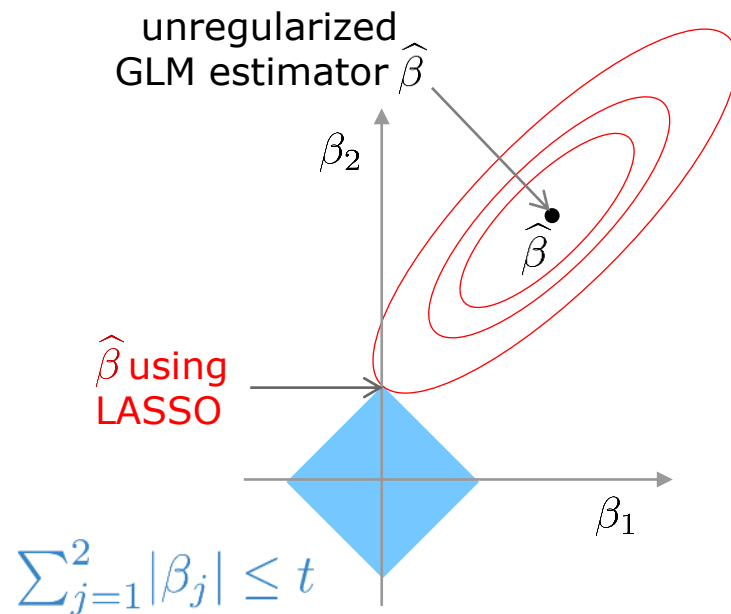
# Now it is Time for an Example

## The LASSO

LASSO: **L**east **A**bsolute **S**election and **S**hrinkage **O**perator (Tibshirani, 1996)

- Penalty Function:  $\ell_1$  norm

$$\Omega(\beta_1, \dots, \beta_m) = \|(\beta_1, \dots, \beta_m)\|_1 = \sum_{j=1}^m |\beta_j|$$



# One Method to Rule Them All

## Allowing for All Types of Variables

- The pricing app makes use of a regularization technique that allows for all types of variables.
- The method was first proposed by the Institute for Financial and Actuarial Sciences (ifa) at the DAV Annual Conference 2019 in Düsseldorf, Germany.



### Main idea (ifa): Regularization of an extremely large design matrix

- Use clever dummy/contrast coding to enable adaptive learning of non-linear structures
- Allow for main effects and interactions
- You think this is too complex?  
→ Bring in the LASSO!



| Age (PH)    | ... | 41 | 42 | 43 | 44 | 45 | ... |
|-------------|-----|----|----|----|----|----|-----|
| 43-year-old | ... | 1  | 1  | 1  | 0  | 0  | ... |
| 44-year-old | ... | 1  | 1  | 1  | 1  | 0  | ... |

Example: Contrast coding for staircase functions



### Options: Remaining model calibration

- Global penalty budget  $\lambda$
- Coding setup per variable: staircase, stepwise linear, or hybrid
- Optional: Manual adjustments per variable



### Result: Data-driven GLM modeling

- Simultaneous and coherent allowance for variables of different types
- Objectively data-driven and increasingly automatized modeling process
- Integrated feature selection, binning, transformations, interactions, ...
- Well-known model output for visualization, interpretation, and integration in existing pricing processes

## **Live Demo**

Motor Case Study with Realistic Data

**Live Demo**

# Thank you for your attention!



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# References

## Literature and Credits

- Literature
  - Devriendt, S., Antonio, K., Reynkens, T., & Verbelen, R. (2018). Sparse Regression with Multi-type Regularized Feature Modeling. arXiv preprint arXiv:1810.03136.
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  - Zou, H., & Hastie, T. (2005). Regularization and variable selection via the elastic net. Journal of the royal statistical society: series B (statistical methodology), 67(2), 301-320.
- Credits
  - All illustrations by courtesy of the Institute for Financial and Actuarial Sciences (ifa) in Ulm, Germany; taken from Lukas Hahn, "Tarifizierung in der Schaden-/Unfallversicherung - Ergänzung klassischer Tarifizierung durch moderne Data-Analytics-Methoden", DAV Annual Conference 2019 in Düsseldorf, Germany, on 25 April 2019, Section "Actuarial Data Science"
  - In addition,
    - for slides 2 and 5: All icons made by Freepik from [www.flaticon.com](http://www.flaticon.com).
    - for slide 3: All icons designed by Showeet.com.
    - for slide 4: Own illustration based on Tibshirani, R., Wainwright, M., & Hastie, T. (2015). Statistical learning with sparsity: the lasso and generalizations. Chapman and Hall/CRC.